

**Tabulation of primes of the form  $k \cdot 2^n + 1$**

Year	Reference	Interval for $k$	Interval for $n$
1958	R. M. Robinson [12]	$1 \leq k < 100$	$1 \leq n < 512$
1977	G. Matthew and H. C. Williams [10]	$1 < k < 100$ $100 < k < 130$	$512 \leq n \leq 1000$ $1 \leq n \leq 1000$
1979	R. Baillie [2]	$1 < k < 130$ $130 < k < 150$	$1000 < n \leq 1500$ $1 \leq n \leq 1500$
1980	G. V. Cormack and H. C. Williams [3]	$1 < k < 30$	$1500 < n \leq 4000$
1980	W. Keller [6]	$1 \leq k < 1200$	$1 \leq n \leq 1000$
1983	W. Keller [7]	$1 < k < 20$ $30 < k < 150$ $150 < k < 200$	$4000 < n \leq 8500$ $1500 < n \leq 4000$ $1000 < n \leq 4000$
1985	H. Suyama [13]	$200 < k < 500$	$1000 < n \leq 2200$
1991	W. Keller [8]	$1 < k < 20$ $20 < k < 32$ $32 < k < 64$ $64 < k < 120$ $200 < k < 500$	$8500 < n \leq 15000$ $4000 < n \leq 15000$ $4000 < n \leq 12000$ $4000 < n \leq 8000$ $2200 < n \leq 2500$
1992	W. Keller [9]	$200 < k < 250$	$2500 < n \leq 4000$
1992	H. Dubner [4]	$120 < k < 220$ $250 < k < 500$ $500 < k < 1200$ $1200 < k < 2200$	$4000 < n \leq 8000$ $2500 < n \leq 4000$ $1000 < n \leq 4000$ $1 \leq n \leq 2000$
1993	H. Dubner [4, 5]	$1 < k < 32$ $32 < k < 64$ $64 < k < 120$ $120 < k < 220$ $220 < k < 1200$ $1200 < k < 2200$ $2200 < k < 3000$ $3000 < k < 20000$ $20000 < k < 40000$ $40000 < k < 100000$ $40000 < k < 100000$	$15000 < n \leq 40000$ $12000 < n \leq 20000$ $8000 < n \leq 20000$ $8000 < n \leq 12000$ $4000 < n \leq 10000$ $2000 < n \leq 3000$ $1 \leq n \leq 3000$ $90 < n \leq 1200$ $90 < n \leq 1000$ $90 < n \leq 400$ $600 < n \leq 1000$

**Tabulation of primes of the form  $k \cdot 2^n + 1$  (continued)**

Year	Reference	Interval for $k$	Interval for $n$
1993	W. Keller [9]	$3000 < k < 100000$ $40000 < k < 100000$	$1 \leq n \leq 90$ $400 < n \leq 600$
1993	J. Young [14, 15]	$1 < k < 32$ $2246 < k < 3000$ $3000 < k < 10000$	$40000 < n \leq 50000$ $3000 < n \leq 5000$ $1200 < n \leq 5000$
1996	A. Björn and H. Riesel [1]	$1 \leq k < 21000$	$1 \leq n \leq 3000$
1996	J. Young [14, 15]	$1 < k < 14$ $14 < k < 32$ $32 < k < 64$ $1 < k < 256$ $1200 < k < 2246$	$50000 < n \leq 200000$ $50000 < n \leq 100000$ $20000 < n \leq 50000$ $100 < n \leq 20000$ $3000 < n \leq 5000$
1997	W. Keller [9]	$21000 < k < 40000$	$1000 < n \leq 3000$
1997	J. McLean [11]	$40000 < k < 100000$	$1000 < n \leq 2000$

**Summary**

Year		Interval for $k$	Interval for $n$
1997	Overall	$0 < k < 14$ $14 < k < 32$ $32 < k < 64$ $64 < k < 256$ $256 < k < 1200$ $1200 < k < 10000$ $10000 < k < 40000$ $40000 < k < 100000$	$1 \leq n \leq 200000$ $1 \leq n \leq 100000$ $1 \leq n \leq 50000$ $1 \leq n \leq 20000$ $1 \leq n \leq 10000$ $1 \leq n \leq 5000$ $1 \leq n \leq 3000$ $1 \leq n \leq 2000$

## References

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